

## CFD MODELLING OF BREAKING AND UNDULAR TIDAL BORES WITH PHYSICAL VALIDATION

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### ABSTRACT

A tidal bore may form during spring tide conditions when the tidal range exceeds 4 to 6 m in a natural estuary with a funnel shaped river mouth and shallow initial water level. The propagation of tidal bores is a highly unsteady turbulent process associated with intensive sediment scouring and mixing. To date, few physical and numerical studies documented the unsteady turbulent process of tidal bore propagation. Recent numerical CFD models lacked careful experimental validations. The present study aims to provide new results on CFD numerical modelling of tidal bore propagation with a wide range of Froude numbers (1.2 to 2.1) and systematic experimental validations. The model solved the incompressible Navier-Stokes equations in its two-phase flow forms using Large Eddy Simulation (LES). Both 2D and 3D simulations were conducted; the inlet turbulence of the 3D models was simulated by a Synthetic Eddy Method (SEM). The physical experiments were based upon an ensemble-average technique, with measurements of water depth and velocity repeated 25 times for each flow condition. The 2D CFD simulations showed good agreement in terms of free-surface elevations with experimental results, for the range of tested Froude numbers. Mesh grid refinement only improved the accuracy for some but not all flow conditions. The 2D velocity data showed qualitative and quantitative agreement, but only at a selective range of vertical elevation beneath the free-surface, where the inlet velocity were correctly reproduced. The 3D simulation highlighted a numerical boundary layer, the thickness of which agreed with the experimental results. The time-averaged velocity and velocity RMS of the numerical model data showed a closer agreement with the physical model outside the boundary layer. The development of the numerical boundary layer was clearly observed in the CFD model results.

**Keywords:** Tidal bores; CFD modelling; large eddy simulation LES; physical model validation; turbulence.

### 1 INTRODUCTION

The propagation of tidal bores is a highly unsteady turbulent process, associated with intensive sediment scouring and mixing. The occurrence of a tidal bore is marked by a steep rise in free-surface propagating upstream. A tidal bore could form during spring tide conditions when the tidal range exceeds 4 to 6 m in a natural system with a funnel shaped river mouth and shallow initial water level (Chanson, 2011) (Figure 1). The strength of a tidal bore is characterised by its Froude number, defined as:

$$Fr_1 = \frac{U + V_1}{\sqrt{g \times \frac{A_1}{B_1}}} \quad [1]$$

where  $U$  is the bore celerity positive upstream,  $V_1$  is the streamwise velocity of the initially steady flow positive downstream,  $g$  is the gravitational acceleration:  $g = 9.8 \text{ m/s}^2$ ,  $A_1$  and  $B_1$  are the cross-sectional area and width respectively for the initially steady flow. When the Froude number is less than unity, a bore cannot form. When the Froude number is between 1 and 1.2-1.3, the bore is undular (Treske, 1994; Koch and Chanson, 2008; Leng and Chanson, 2016a). When the Froude number exceeds 1.3-1.5, the bore is breaking, and its strength increases with increasing Froude number (Hornung et al., 1995; Koch and Chanson, 2009; Chanson, 2010; Leng and Chanson, 2016a).

To date, limited physical studies studied the unsteady turbulent propagations of tidal bores (Hornung et al., 1995; Koch and Chanson, 2009; Chanson, 2010; 2011; Docherty and Chanson, 2012; Khezri and Chanson, 2012b; Leng and Chanson, 2015a; 2015b; 2016a; 2017). Recent numerical studies were performed using Computational Fluid Dynamics (CFD) models (Furuyama and Chanson, 2010; Lubin et al., 2010a, 2010b; Reichstetter, 2011; Simon et al., 2011; Chanson et al., 2012; Khezri, 2014; Simon, 2014), albeit over a limited range of Froude numbers and most studies lacked careful experimental validations. The present work

presents new results on a numerical CFD model of the unsteady turbulent propagations of tidal bores in open channel flows, with a wide range of Froude numbers (from 1.2 to 2.1). Both two-dimensional and three-dimensional CFD models were simulated. The modelling results were validated against physical experiments conducted systematically for the exact flow conditions used in the CFD models. The experiments were performed in a 19 m long and 0.7 m wide rectangular prismatic channel. Ensemble-averaged flow measurements were performed, where experiments were repeated 25 times for each controlled flow conditions and the results were ensemble-averaged. The free-surface variations were measured by a series of acoustic displacement meters (ADMs) along the channel centerline, and the velocity characteristics were measured using a Nortek™ Vectrino+ acoustic Doppler velocimeter (ADV). All instruments were sampled at 200 Hz and synchronized within  $\pm 0.01$  s.



(a) Breaking tidal bore of Qiantang River (Laoyanchang, China), photograph taken on 23 September 2016.



(b) Undular tidal bore of Dordogne River (St. Pardon, France), photograph taken on 2 September 2015.

**Figure 1.** Photographs of tidal bores in rivers.

## 2 NUMERICAL METHOD AND CFD MODEL CONFIGURATION

### 2.1 Numerical method and implementation

The numerical modelling was conducted using the CFD code Thétis developed by the I2M laboratory, University of Bordeaux, France. The model solves the Navier-Stokes equations in its incompressible two-phase flow form between non-miscible fluids. In this case, the two fluids were air and water, respectively. A phase function  $C$ , called the color function, is used to locate the different fluids with  $C = 0$  in the air,  $C = 1$  in water, with  $C = 0.5$ , the value assumed to characterise the interface location. The governing equations are presented below, which is the Large Eddy Simulation (LES) of an incompressible fluid flow classically derived by applying a convolution filter to the unsteady Navier-Stokes equations:

$$\nabla \cdot \bar{\mathbf{u}} = 0 \quad [2]$$

$$\rho \left( \frac{\partial \bar{\mathbf{u}}}{\partial t} + \bar{\mathbf{u}} \cdot \nabla \bar{\mathbf{u}} \right) = -\nabla p + \rho \bar{\mathbf{g}} + \nabla \cdot (\mu + \mu_t) [\nabla \bar{\mathbf{u}} + \nabla^T \bar{\mathbf{u}}] \quad [3]$$

and,

$$\frac{\partial C}{\partial t} + \bar{u} \cdot \nabla C = 0 \quad [4]$$

where  $\bar{u}$  is the velocity,  $C$  is the phase function,  $t$  is the time,  $p$  is the pressure,  $\bar{g}$  is the gravity vector,  $\rho$  is the density,  $\mu$  is the dynamic viscosity and  $\mu_t$  is the turbulent viscosity. The turbulent viscosity,  $\mu_t$  is calculated with the Mixed Scale model (Sagaut, 2006), which was found to be accurate for coastal applications (Helluy et al., 2005; Lubin et al., 2006). The magnitude of the physical characteristics of the fluids was calculated based upon the phase function as:

$$\rho = C \times \rho_1 + (1 - C) \times \rho_0 \quad [5]$$

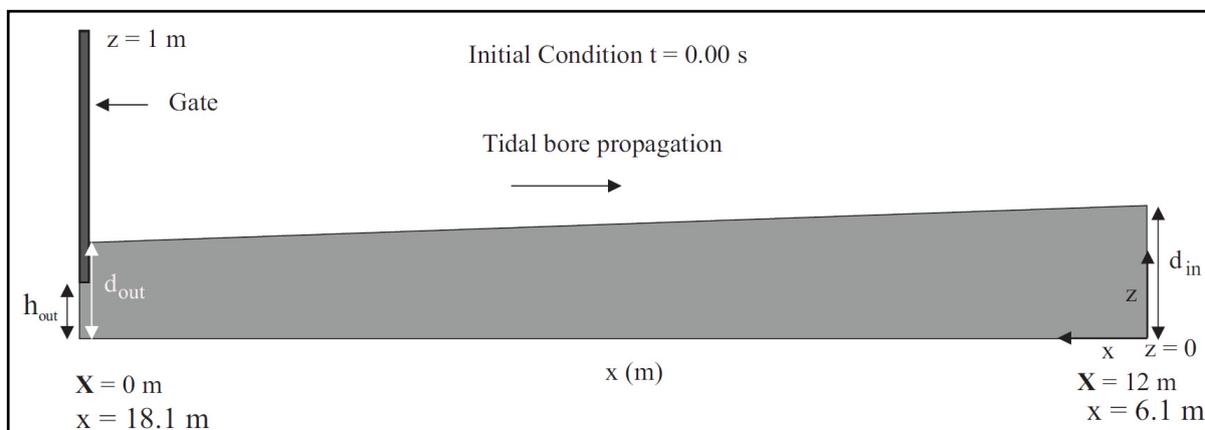
$$\mu = C \times \mu_1 + (1 - C) \times \mu_0 \quad [6]$$

The densities  $\rho_0$ ,  $\rho_1$  and dynamic viscosities  $\mu_0$ ,  $\mu_1$  are the respective properties of fluids 0 and 1: in this case, air and water, respectively. The velocity and pressure coupling is solved with a pressure correction method (Goda, 1979).

The space derivatives of the inertial term are discretised by a hybrid upwind-centered scheme and the viscous terms is approximated by a second-order centered scheme (Lubin et al., 2006). The interface tracking was done using a Volume of Fluid (VOF) method with a piecewise linear interface calculation (PLIC). This method has the advantage of building a sharp interface between air and water. The time discretization is implicit and the equations are discretised on a staggered grid thanks to a finite volume method. The MPI library HYPRE was used to solve the linear system of the prediction and correction steps (Falgout et al., 2006). The time steps were dynamically calculated to insure a CFL condition inferior to 0.2. The numerical model has been proved accurate through a variety of coastal applications and numerous test cases (Lubin, 2004; Lubin et al., 2006). Earlier CFD studies of tidal bores by Simon et al. (2011) and Khezri (2014) were also based upon this model.

## 2.2 Numerical model configuration

Both 2D and 3D CFD simulations were conducted in the present study. For 2D CFD simulations, breaking bores of  $Fr_1 = 1.5$  and  $2.1$ , and undular bores of  $Fr_1 = 1.2$  were modelled numerically. The numerical domain was 12 m in the longitudinal (stream-wise) direction and 1 m in the vertical direction (Figure 2). A no-slip condition was imposed at the lower boundary ( $z = 0$  m) and a Neumann condition was used at the upper boundary ( $z = 1$  m). At the end of domain ( $x = 12$  m), a wall boundary was imposed to act like a closed gate to reproduce the experimental generation process. The opening under the gate  $h_{out}$  could be set to introduce a Neumann condition between the bed ( $z = 0$  m) and the bottom of the gate ( $z = h_{out}$ ). The initial conditions of the 2D models consisted of a water trapezoid, with higher depth at the inlet ( $d_{in}$ ) and lower depth at the outlet ( $d_{out}$ ) to approximate the gradually-varied flow in the physical open channel. All initial and boundary parameters were taken from the experimental measurements.



**Figure 2.** Definition sketch of numerical domain configurations;  $X$  is the distance from the left boundary (i.e. gate) of the numerical domain;  $x$  is the distance from the upstream end of the physical channel.

For 3D CFD simulations, the work is still in progress. Herein, only data of the initially steady flow before the bore arrival will be presented. The flow conditions simulated by the 3D CFD model corresponded to the initially steady flow before the breaking bore of  $Fr_1 = 2.1$ . The 3D model was based upon the 2D model configuration, extruded in the third direction being the transverse  $y$  dimension. The coordinate  $y$  was positive

towards the left side wall and the 3D numerical domain was 0.7 m wide. In this case, no-slip conditions were applied to both lateral walls and bottom of the domain. The Synthetic Eddy Method (SEM) was used in the 3D model to inject turbulence at the inlet of the domain (Jarrin et al., 2006; 2009). The input parameters for this method, including mean velocity and velocity fluctuations, were all extracted from the experimental data of Leng and Chanson (2016a). The number of eddies was set at 2000 and the size of eddies was 0.010 m, which was an order of magnitude higher than the experimental data (Leng and Chanson, 2017). Jarrin et al. (2006; 2009) found that the method gave better results with over-estimated eddy size. Table 1 documents detailed configurations of the 2D and 3D numerical models. In the table,  $S_o$  stands for the channel slope in the longitudinal direction. The opening under the gate after rapid closure is denoted  $h_{out}$ .

Table 2 summarises the experimental flow conditions corresponding to the three Froude number modelled by CFD ( $Fr_1 = 1.2, 1.5, 2.1$ ). The reference depth,  $d_1$  and celerity,  $U$  was taken at the velocity sampling location, which was located 9.6 m upstream of the gate for both physical and numerical channels.

**Table 1.** Initial configuration of the 2D and 3D numerical simulations.

Reference	Domain (m)	Mesh grid density	$Fr_1$	$Q$ ( $m^3/s$ )	$S_o$	$d_{in}$ (m)	$d_{out}$ (m)	$h_{out}$ (m)	Bore type
2D_Fr1.2	12×1	1600×100	1.2	0.101	0	0.208	0.19	0.071	Undular
2D_FR1.5	12×1	2400×200	1.5	0.101	0	0.18	0.16	0	Breaking
2D_FR2.1	12×1	1600×140	2.1	0.101	0.0075	0.1	0.1	0	Breaking
3D_FR2.1	12×1×0.7	1600×250×200	2.1	0.101	0.0075	0.093	0.093	0	Breaking

**Table 2.** Flow conditions of the experimental data used to validate the numerical model.

Reference	$Fr_1$	$Q$ ( $m^3/s$ )	$S_o$	$d_1$ (m)	$U$ (m)	Bore type	Instrumentation
Leng and	1.2	0.101	0	0.210	0.71	Undular	ADMs and ADV
Chanson	1.5	0.101	0	0.180	1.13	Breaking	ADMs and ADV
(2016a)	2.1	0.101	0.0075	0.100	1.00	Breaking	ADMs and ADV

### 3 2D SIMULATION OF TIDAL BORE PROPAGATION

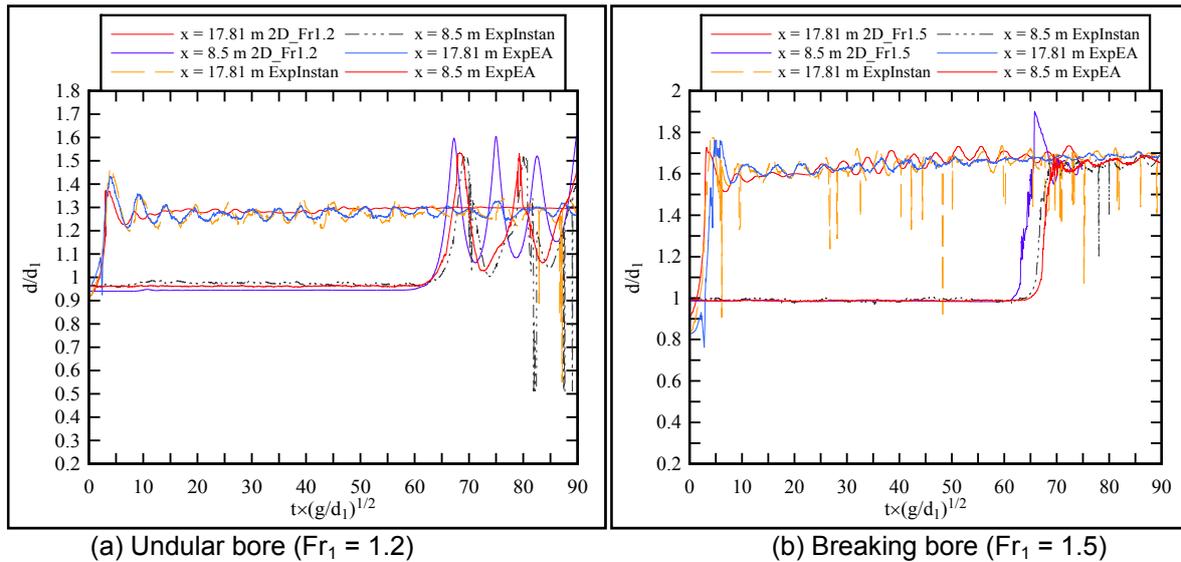
#### 3.1 Free-surface comparisons

During the physical experiments, both instantaneous and ensemble-averaged measurements were performed to characterise the free-surface and velocity properties. Up to 10 acoustic displacement meters (ADMs) were installed at different longitudinal positions  $x$  ( $x$  = longitudinal distance from upstream end) on the channel centerline, all sampling at 200 Hz, to record the free-surface variations with time at different locations along the channel. During the numerical simulations, the free-surface variations with time were recorded at the same locations as those of the ADMs to validate the numerical results. Comparisons between numerically simulated free-surface evolution and experimental observations were conducted, and typical results are presented in Figure 3 for both undular and breaking bores. Note that the gate was located at  $x = 18.1$  m.

Overall, the free-surface variations simulated by the 2D CFD model agreed well with the experimental data (instantaneous or ensemble-averaged) at all longitudinal locations, quantitatively and qualitatively, for all Froude numbers. Some deviations were observed in terms of the bore height and bore celerity. At generation (close to the gate), the numerical model tended to estimate relatively accurately the free-surface rise mechanism, with almost identical depth gradient with time. However, the bore height was underestimated for both breaking and undular bores at generation. As the bore propagated upstream towards mid-channel, the numerical model overestimated the bore celerity and bore height, resulting in differences in terms of bore arrival time at  $x = 8.5$  m (Figure 3). For undular bores, the numerical model was associated with secondary wave periods which differed from the experimental data. The wave forms of the numerical model appeared to be more regular than the experimental data, due to the two-dimensional constraint and the absence of side wall effects.

#### 3.2 Velocity comparisons

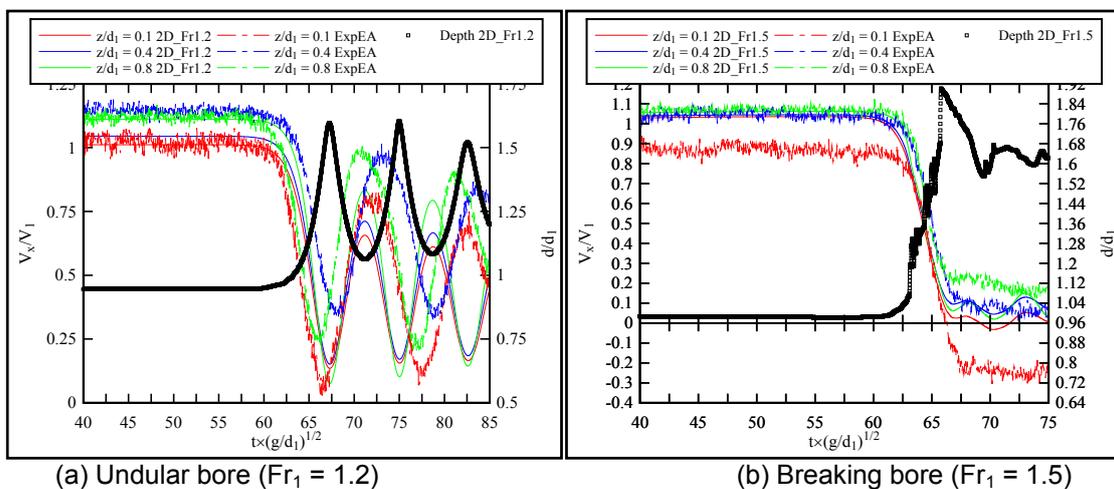
Ensemble-averaged velocity measurements were performed using a Nortek™ Vectrino+ acoustic Doppler velocimeter (ADV) located on the channel centerline at mid-channel ( $x = 8.5$  m). The ADV was equipped with a three-dimensional side looking head, able to record velocity in the longitudinal, transverse and vertical directions. The ADV was sampled at 200 Hz, synchronised with the ADMs, and measured velocity at a number of vertical elevations ( $z/d_1 = 0.1, 0.4, 0.8$ ). During the numerical CFD modelling, velocity data at the same dimensionless vertical elevations was recorded at  $x = 8.5$  m for validation purposes. Figure 4 presents typical comparisons between numerical and experimental results for bores with  $Fr_1 = 1.2$  and 1.5. The time frames of the numerical and experimental data was synchronized using the numerical time line.



**Figure 3.** Dimensionless free-surface time evolution for undular and breaking bores of  $Fr_1 = 1.2$  and  $1.5$ , respectively; Comparisons between numerical simulation (2D\_Fr), instantaneous experimental data (ExpInstan) and ensemble-averaged experimental data (ExpEA).

Overall, the time-variations of the numerically-simulated velocity data agreed well with the experimental data at all vertical elevations and for all velocity components. The longitudinal velocity was associated with a sharp deceleration following the arrival of breaking bores. The vertical velocity showed a sharp acceleration, then deceleration, following the breaking bore arrival. One feature which was absent from the numerical data set was the presence of a boundary layer in the initially steady flow as shown in the experimental results. Although a no-slip condition was imposed at the bottom boundary of the model, resulting in slightly lower steady flow velocity for lower vertical elevations (Figure 4), no obvious boundary layer such as highlighted in the experimental data was observed. This would be further addressed in the 3D simulation documented in Section 4.

Despite the absence of boundary layer, the present numerical data highlighted some longitudinal recirculation at the lowest vertical elevation during the propagation of breaking bores with complete gate closure (Figure 4b). Field and experimental studies have documented the presence of longitudinal recirculation next to the bed (often  $0 < z/d_1 < 0.3-0.5$ ) beneath the bore front of both the breaking and undular bores (Wolanski et al., 2004; Chanson and Toi, 2015; Leng and Chanson, 2016a). This is characterised by a negative longitudinal velocity at the end of the deceleration following the bore passage, highlighted by the experimental data of breaking bores at  $z/d_1 = 0.1$  in Figure 4b. At the same dimensionless vertical elevation next to the bed, the numerical data showed qualitatively some longitudinal recirculation velocity, however, with a time delay and lesser strength (red solid curve in Figure 4b).



**Figure 4.** Dimensionless time-variations of longitudinal velocity for undular and breaking bores of  $Fr_1 = 1.2$  and  $1.5$ , respectively; Comparisons between numerical simulation (2D\_Fr) and ensemble-averaged experimental data (ExpEA).

The undular bore was characterised by a gentle free-surface rise, followed by a series of well-formed secondary waves. Meanwhile, the longitudinal velocity decreased in a smooth manner with the rise of free-surface, and oscillated quasi-periodically with the free-surface by a phase difference of  $\pi$ . The vertical velocity increased with the free-surface rise, then oscillated quasi-periodically with the free-surface by a phase difference of  $\pi/2$ . The numerical results reproduced the periodic oscillations in the free-surface, longitudinal and vertical velocity variations, however, with periods different from the experimental data. More specifically, the numerical data was associated with a shorter period. The minimum longitudinal velocity reached by the numerical model was higher than the experimental data, whereas the maximum longitudinal velocity of the secondary waves was lower than the experimental data (Figure 4). The difference was believed to be due to the lack of the third dimension and of sidewall friction, and hence resulting in a more energetic behavior of the bore.

### 3.3 Discussion

The 2D numerical modelling results showed large vortical structures formed both underneath and behind the front of breaking bores (Figure 5). Previous 2D CFD modelling by Khezri (2014) observed large vortical structures formed close to the bed, with a vertical dimension  $L_z$  up to 0.1 m ( $L_z/d_1 \approx 0-0.5$ ) underneath breaking bores of Froude number 1.5. The present study highlighted two types of vortical structures, one near the fluctuating free-surface behind the roller, and one close to bed. The vortical structures near the upper free-surface were observed almost immediately downstream of the breaking roller, with length scales of  $L_x \approx 0.1$  m ( $L_x/d_1 \approx 0.56$ ), and were advected downstream as the bore front propagated upstream. This type of vortical structures were formed by the plunging mechanism of the steepened bore front into the flow and was typically associated with pockets of air.

The vortical structures next to the bed were observed to be flat and elongated, with much larger length scales in the longitudinal direction compared to the vertical direction. The height of these vortical structures was approximately  $L_z \approx 0.02$  m ( $L_z/d_1 \approx 0.11$ ). Experimental studies of turbulent scales by Leng and Chanson (2017) highlighted presence of anisotropic vortical structures underneath the bore front. The vertical length scale  $L_z$  was up to 0.02 m ( $L_z/d_1 \approx 0-0.11$ ) for breaking bores with relatively large Froude numbers ( $Fr_1 \geq 1.5$ ). The numerical results agreed with the experimental findings in terms of the vertical length scale of the vortical structures near the bed. The occurrence of vortical structures in the numerical model was found to be approximately 1 m downstream of the bore front, which was greatly delayed compared to experimental observations and past numerical results. The reason could be due to the 2D constraint, where bubble breakup mechanism was not allowed. Some numerical air bubbles were still observed more than 2 m ( $\Delta x/d_1 \approx 0-11$ ) following the leading edge of the bore, while the entrained bubbles would have risen to the free-surface in a real physical flow (Wang et al., 2016).

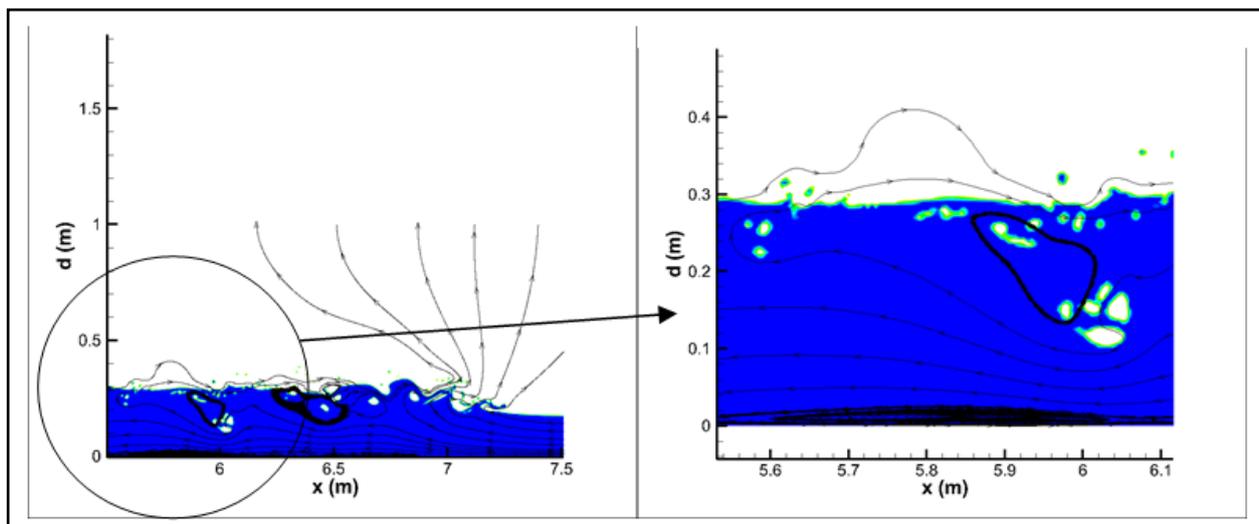
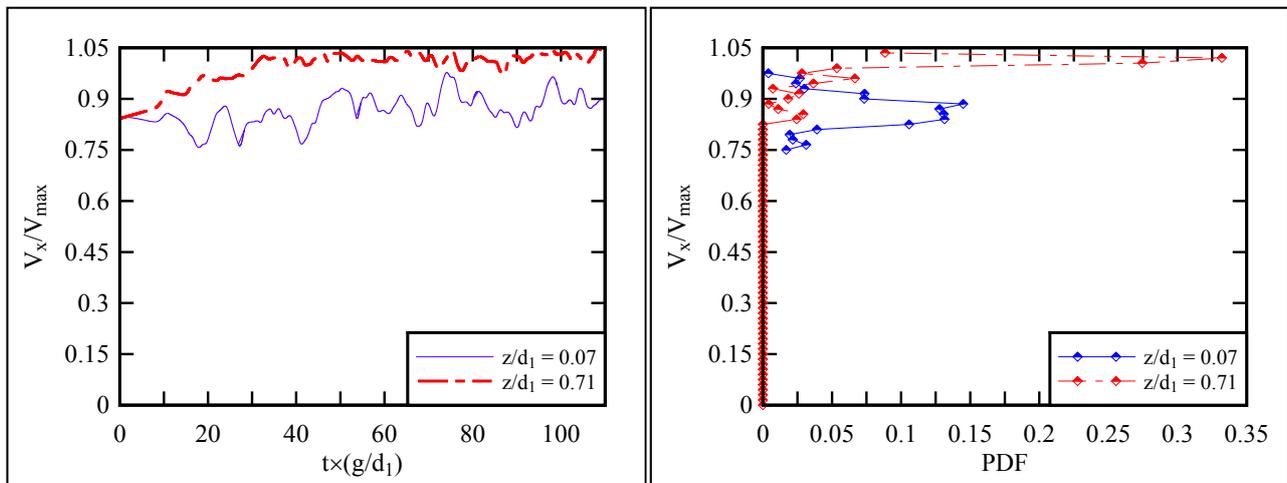


Figure 5. Vortical structures observed beneath the tidal bore.

## 4 3D STEADY FLOW SIMULATION

Figure 6 presents typical time series and PDFs of the longitudinal velocity components simulated at  $x = 8.5$  m by the 3D CFD model (3D\_Fr2.1) in steady flow at two different vertical elevations  $z$ . The 3D CFD model was run for a physical time span of 10.609 s (dimensionless time  $t \times (g/d_1) \sim 110$ ), and the turbulence arrived at the velocity sampling location approximately after 1 s (dimensionless time  $t \times (g/d_1) \sim 10$ ). Compared to the 2D results in the steady flow phase (Figure 3 and 4), the present 3D results clearly highlighted some turbulent fluctuations in all velocity components at all vertical elevations. Moreover, from the time series and

PDFs, variations in longitudinal velocity magnitudes with vertical elevations can be observed. Namely, the mean velocity at higher vertical elevation ( $z/d_1 = 0.71$ ) was larger than that at lower elevation ( $z/d_1 = 0.07$ ). This indicated the successful reproduction of a turbulent boundary layer.

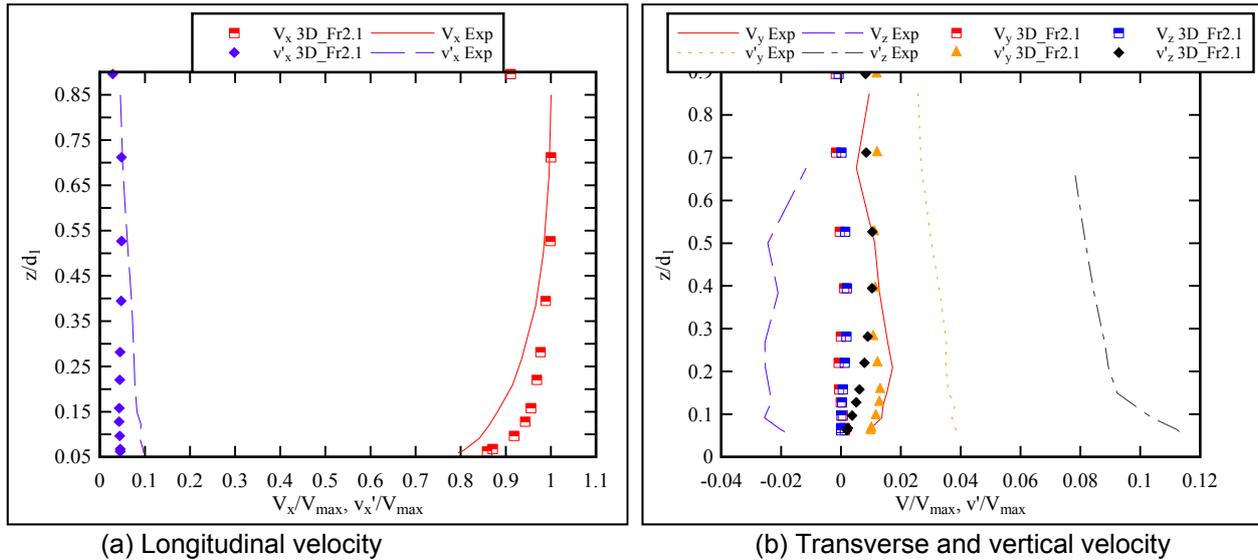


(a) Time-variations of instantaneous longitudinal velocity (b) PDF of longitudinal velocity  
**Figure 6.** (a) Time-variations of the instantaneous longitudinal velocity simulated at  $x = 8.5$  m,  $z/d_1 = 0.07$  and  $0.71$  by the numerical model (3D\_Fr2.1); (b) the corresponding probability density functions at two vertical elevations.

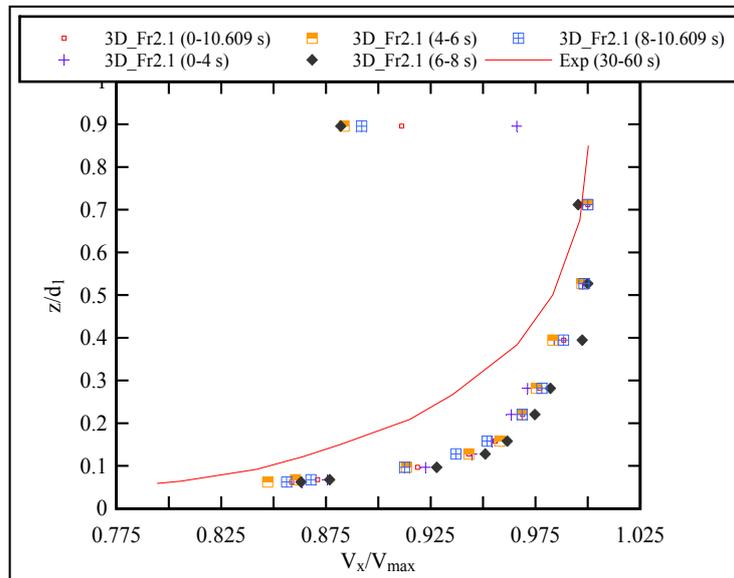
Figure 7 presents the vertical profile of the time-averaged velocity  $V$  and velocity fluctuations  $v'$  simulated at  $x = 8.5$  m. The numerical results were compared to the experimental data. The numerical results were time-averaged over the entire 10.609 s time span. The experimental data was time-averaged over 30 s. As highlighted by Figure 7a, the numerical profile of the longitudinal velocity clearly showed a bottom boundary layer. The vertical profile of the longitudinal velocity simulated by the numerical model agreed well in shape and values with the experimental data, especially at the outer edge and outside of the boundary layer, except for the highest vertical elevation. Inside the boundary layer, the numerical data agreed better with the experimental data close to bed, then deviated from the experimental curve, before they coincided again near the outer edge. The longitudinal velocity fluctuations, highlighted by its standard deviation, agreed quantitatively and qualitatively with the experimental data, with better fit near the outer edge and outside of the boundary layer.

The vertical profile of the transverse and vertical velocity components simulated by the numerical model showed very small, near-zero magnitudes (Figure 7b). The values were orders of magnitudes smaller than the experimental data throughout the vertical range. The velocity fluctuations in the transverse and vertical directions were associated with values higher than the corresponding velocity component magnitudes, highlighted by the numerical data. Furthermore, the numerical data showed increase in velocity fluctuations with increasing vertical elevations, which agreed in terms of trend with the experimental data. Nevertheless, the experimental fluctuations were orders of magnitudes higher than the numerical ones, especially in the vertical direction. This could be attributed to the arrangement of the ADV head, which was known to over-estimate the vertical velocity fluctuations because of beam reflections and echo effects on the bed.

From the time series, turbulence was observed to arrive at the velocity sampling point after approximately 1 s and was fully developed after 5 s. The evolution of the numerical boundary layer was thus studied by time-averaging the longitudinal velocity at different vertical elevations over different time spans, from the entire time span of 10.609 s down to every 2 s. The results are presented in Figure 8, with comparison to experimental data. Overall, all numerical profiles were associated with the presence of boundary layers. The point at the highest vertical elevations ( $z/d_1 = 0.90$ ) was associated with outlying values at all time. This was previously observed by Simon (2014) using the same numerical tool. For all time spans, the numerical data showed better agreement near the bottom and close to the outer edge of the boundary layer. Throughout the vertical range, the accuracy of the data seemed to be unaffected by the time span over which the numerical data was averaged, as long as the turbulence has reached the velocity sampling location. The findings seemed to suggest that, once the flow became turbulent and the boundary layer started to develop in the numerical model, the steady flow data would not evolve with longer time of simulation. The finding indicated good quality of numerically simulated turbulence, and highlighted the importance of using the actual experimental data for the numerical inlet boundary.



**Figure 7.** Vertical time-averaged velocity profile of the steady flow longitudinal (a), transverse and vertical (b) velocity components at  $x = 8.5$  m; Comparison between numerical (3D\_Fr2.1) and experimental results (Exp).



**Figure 8.** Vertical profile of time-averaged longitudinal velocity at  $x = 8.5$  m, simulated by the numerical model and averaged over different time span (3D\_Fr2.1).

## 5 CONCLUSIONS

The propagation of tidal bores in open channels was investigated numerically using 2D and 3D CFD model with Large Eddy Simulations. The numerical modelling investigated tidal bores with Froude numbers ranging from 1.2 to 2.1. The results of the numerical studies were compared and validated against experimental data collected under the same flow conditions. Overall, the 2D numerical results gave good approximation of the free-surface elevation associated with the bore propagation for the range of Froude numbers. The modelled velocity data agreed well with the experimental data outside the boundary layer, and highlighted some longitudinal recirculation underneath breaking bores, although with a delayed occurrence. The numerical model tended to over-estimate the bore celerity and under-estimate the bore height for both breaking and undular bores. Streamline tracing of the numerical results highlighted elongated thin vortical structures behind the bore front and close to bed, with vertical length scale comparable to experimental findings. The 3D steady flow results highlighted a developing boundary layer in the initially steady flow before the bore generation. The thickness of the boundary layer was comparable to experimental results, and the numerical and experimental velocity profiles agreed closely next to the bottom and near the outer edge of the boundary layer. The development of the numerical boundary layer over time was examined. Results suggested that after the turbulence has reached the velocity sampling location, the numerical boundary layer changed very little with longer simulation time.

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